



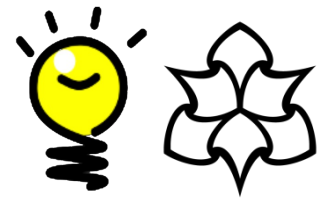
# ***Combining Constraint-Based and Imperative Programming in MABS for More Reliable Modelling***

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(long-term work in parallel to Gary Polhill,

*James Hutton Institute*)



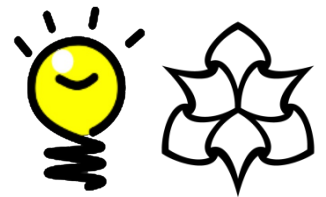
# Motivation

# Did you ever do any of the following?

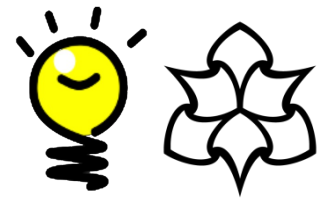


- Write some fairly arbitrary code because, although some characteristics of the target process are known, many details are not
- Use a random generator to add noise into a simulation and then average the results, hoping this gives you a good idea of outcomes
- Fail to add in sufficient internal checking and tests because it messes up your code
- Reimplement standard entities, not knowing if you did this in exactly the same way as others

# Did you ever do any of the following?

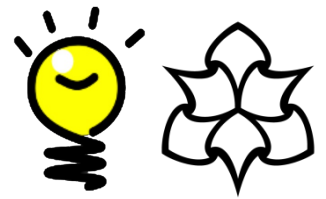


- Implement different aspects of a simulation based on accounts by domain experts, but with no formal check on their consistency
- Import a sub-model that someone else developed and tested, but had no check it was working correctly
- Look at someone else's simulation and be unclear which parts are essential core assumptions and which are more contingent implementation choices



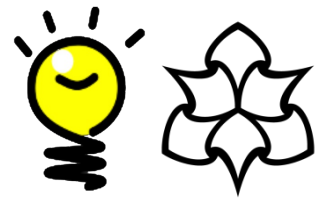
# Some Relevant Existing Work to Generalise From

# Strong Type Checking



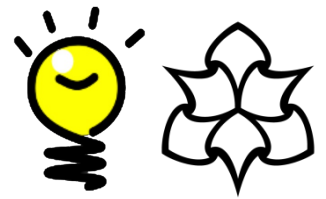
- Constrains variables to only be able to contain the right kind of data
  - e.g. a list of strings, a positive integer
- Checks both syntactically in the code as well as during run time
- Prevents some subtle bugs
- The information is often embedded within the code and hard to separate out
- Limited in what checking it can do

# Stubs



- Temporary code one puts into a model so you can program and test other parts
- Often specifies some null or random behaviour
- Needed with complex models with different interrelated parts
- Later revisited and fleshed out
- This is a matter of degree, often MABS have stub-like elements for some aspects
- Some are just left in the code as they are!

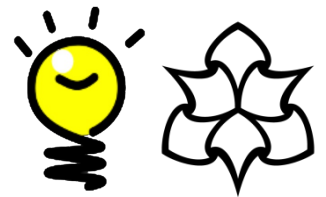
# Random Number/Choice Generators



- Often used when:
  - We do not understand how to code the particular behaviour
  - In stubs, as a temporary measure
  - As “noise” to explore robustness etc.
  - We think the process does not matter to results
- But these only sample possibilities
- Different kinds of generator have their own properties which may drive results

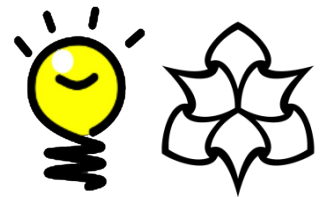


# Formal Ontologies



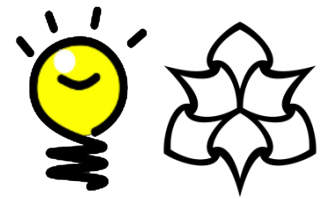
- Defines the agreed entities (both abstract and observed) with a set of labels
  - e.g. money, person, household, field, norm...
- Defines the important, definitional relationships between these
  - e.g. a household is a set of people, a farm is a farmer plus a set of fields
- There are tools to formalise these logically
- Difficult to get agreement upon these!
- It was hoped useful things could be inferred from these, but such inference was ‘thin’

# APIs

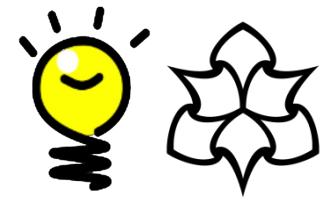


- A precise description of how a unit of code (agent, module, procedure) should interact with the rest of the code
- Agreed between people/tasks so these can be separated out
- If something abides to its API one does not have to understand how it works inside
- Checking some code does abide to its API is difficult and time consuming

# Internal and Unit Tests

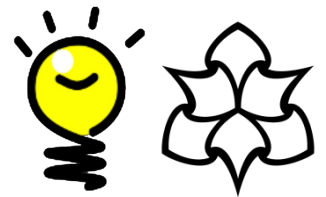


- In more complex simulations there is always a danger of hidden bugs/mistakes
- Thus, it is good practice to program in lots of internal checks to catch some of these
  - e.g. that there are never any negative prices
- Unit tests are a suite of tests that checks the standard behaviour of some code, which can be run when the code is changed
- Once assured they can be switched off
- Can be embedded in the code, so hard to find



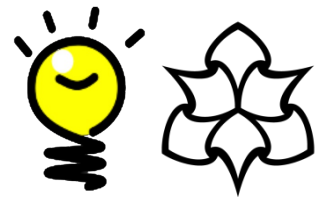
# Integrated but Seperable Declarative and Imperative Layers

# Declarative vs Imperative Programs



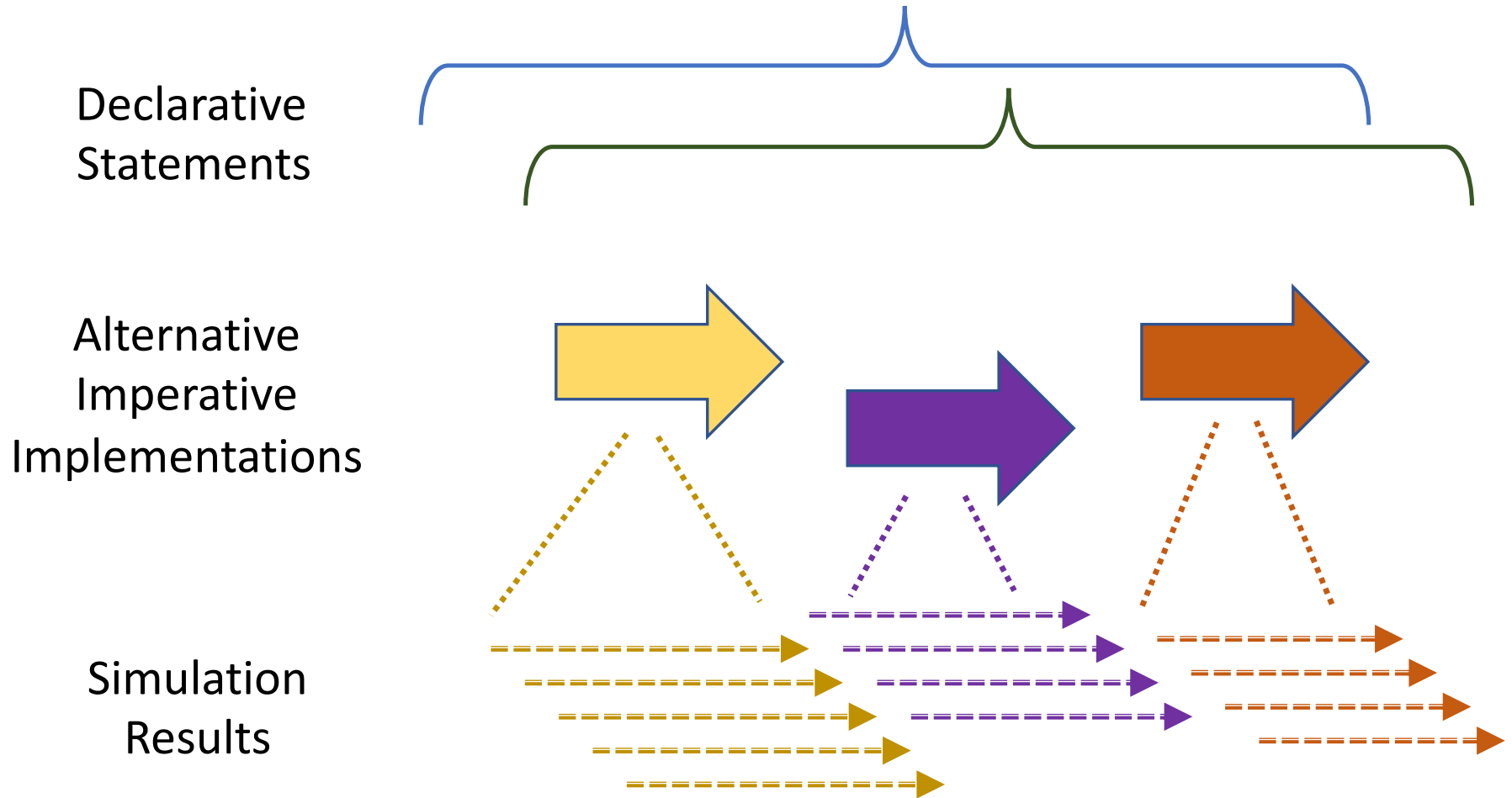
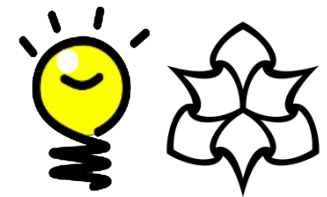
- In **imperative programs** (NetLogo, python, R...) one specifies (at the micro-level) what steps in a process should be done in turn – the computer then does these in that order
- In **declarative programs** (Prolog...) one writes a set of statements, specifying states and relationships, and the computer finds a computation that is consistent with these
- In **constraint programming** this is optimised for combinotronic problems

# The Main Idea

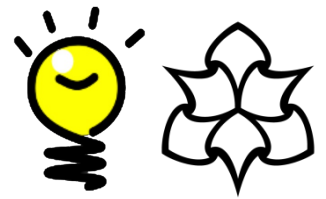


- Separable declarative and imperative “layers” describing the *same* simulation
- Declarative layers may include standard specifications decided by community
- Early execution using declarative layer with minimum of generators added
- Gradually more imperative details added in (where these are known)
- When all is checked, imperative layer only can be executed for speed/sensitivity etc.

# Different “Layers” of a Simulation



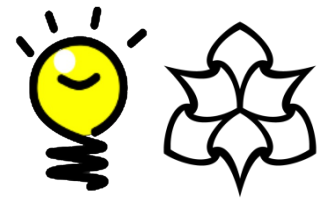
# Possible Programming Sequence



1. Ontology
2. Key assumptions
3. Extended checking
4. Generators and fillers
5. Add in imperative details gradually
6. Turn off declarative layer for speed, sensitivity analysis

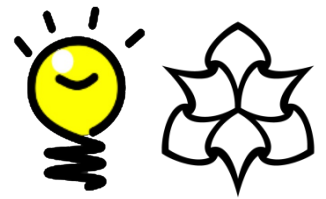


# Advantages of the approach



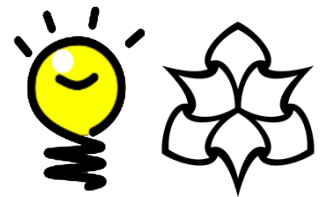
- Joining models
- Comparing models
- Enhanced error checking
- Reusable modules/specifications
- Rapid prototyping
- Support more automation of modelling
- Separation of specification and implementation
- Possibility of exploring all behaviours that satisfy the constraints (albeit inefficiently)
- Declarative layer may include information to inform efficient meta-computation (parallelism/surrogates)

# Disadvantages of the approach

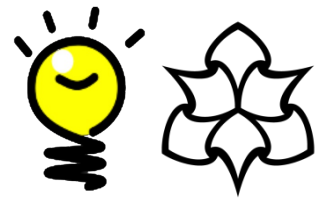


- We do not yet have such a system
- More technical machinery to get one's head around
- Purely declarative execution will be slow
- Spoiling modellers' fun by making modelling more of a formal process
- To leverage the most advantage from this architecture the community needs to agree on some declarative specifications

# Some Previous Work

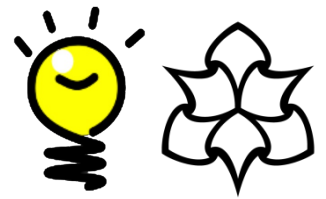


- A strictly declarative modelling language, SDML (Moss & al. 1998, Edmonds & al. 2002)
- ...and its use for constraint exploration (Terán et al. 2001, 2002)
- Importance of ontologies for socio-ecological system modelling (Polhill & Gotts 2009, Gotts & al. 2019)
- A NetLogo extension for extracting an ontology from a model (Polhill 2015)
- A declarative simulation architecture – “OBIAMA” – based on ontologies (Polhill 2016)



# An Example

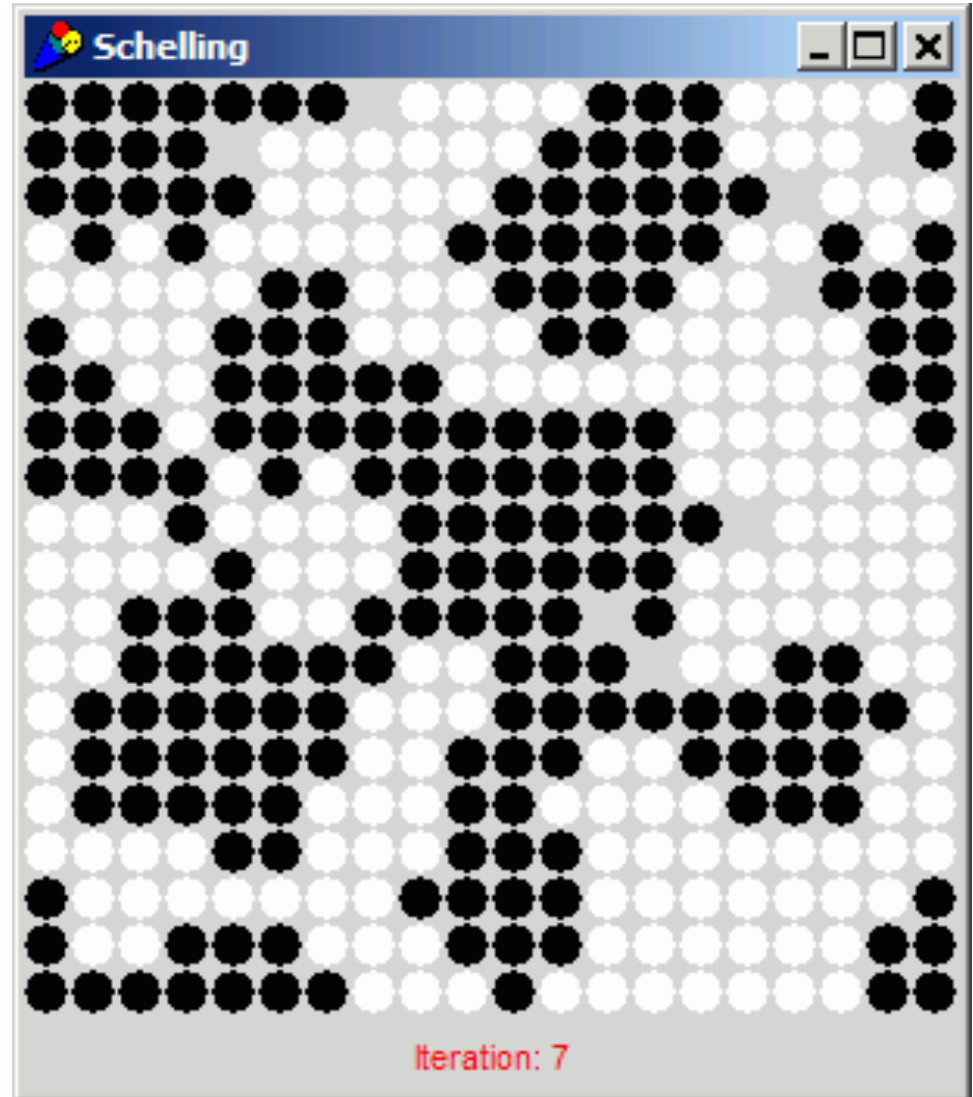
# The Sakoda/Schelling Model (again 😊)



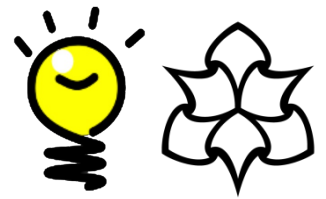
**Setup:** agents, which are in neighbourhoods and have a property, some spaces left empty.

**Dynamic Rule:** repeatedly: each agent looks at its neighbourhood and if not sufficiently similar to self, it moves to an empty square.

**Key Conclusion:**  
Segregation can result from wanting only a few similar neighbours

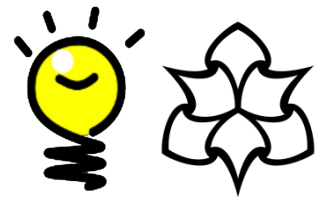


# The *specific* assumptions in the standard 2D Schelling model...



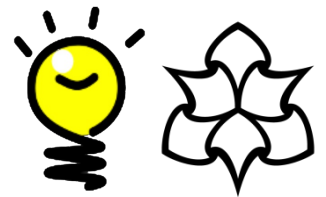
- Agents have one of two colours
- Fixed equal numbers of agents with each colour
- Leaving some spaces
- Randomly placed at set-up on a 2D grid
- Neighbourhoods = Moore Neighbours
- Sufficiently similar = proportion of other agents in neighbourhood with same colour as self  $>$  a parameter
- If moves, destination = random empty square
- Synchronous update (all agents check each time click)
- Segregation = average proportion of neighbours are same colour as self over all agents

# Declarative Entity Specification



- Entities: “locations” with property and agent-occupier/empty
- Entities: Agents with a property and location
- Constraint: each location has at most one agent with its location = self
- Constraint: where agents think they are matches what occupiers locations think they have
- Constraint: there are always some empty? locations

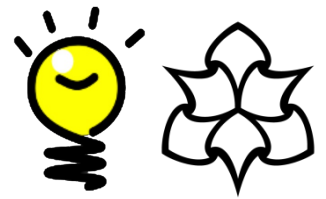
# Dynamics



- Dynamic function:  $\text{Satisfaction}(\text{agent}) \rightarrow \text{Boolean} = \text{predicate}(\text{properties of } (\text{agents}@ \text{neighbourhood}(\text{location}(\text{agent}))))$
- Constraint:  $\text{predicate}(\text{all properties same as self}) = \text{true}$
- Constraint:  $\text{predictate}(\text{no properties same as self}) = \text{false}$
- Update process for an agent:
  - if not  $\text{satisfaction}(\text{agent})$  then
    - next time:  $\text{location}(\text{agent}) \leftarrow$  one of empty locations
    - Next time: that location set to not empty?



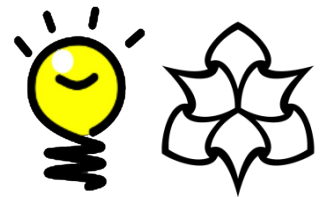
# Space is Complex!



There are different ways of defining neighbourhoods/space, each with subtle consequences! For example define...

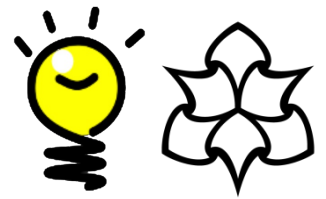
1. given a network of links between locations, neighbourhoods are all locations  $N$  links, or less, away
2. given a distance metric between locations, neighbourhoods are all locations  $<$  set-distance away
3. given a distance metric between locations, neighbourhoods are  $N$  locations closest in distance
4. any of the above then randomly add 10% of agents into an otherwise distant neighbourhood

# Defining Neighbourhoods



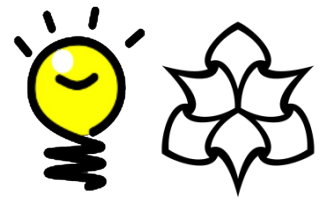
- Locality seems important in this model, but intuitions about space include many aspects
- Fixed neighbourhood function: location  $\rightarrow$  subset of locations
- But which properties of neighbourhoods are essential for the stated results?
  - Constraint:  $\text{dist}(A \rightarrow B) + \text{dist}(B \rightarrow C) \geq \text{dist}(A \rightarrow C)$  (triangle inequality) ??
  - Constraint: many of your neighbours' neighbours are your neighbours (clustering) ??

# Measuring Segregation of Model State



- Function:  $\text{seg}(\text{model}) \rightarrow [0, 1]$
- Constraint: If all agents only have own property in neighbourhoods,  $\text{seg}(\text{model})=1$
- Constraint:  $\text{seg}(\text{model}) \geq \text{seg}(\text{model}')$ , where  $\text{model}'$  has two agents swapped so that the number of links between similar agents increase
- But lots of specific ways of measuring this!

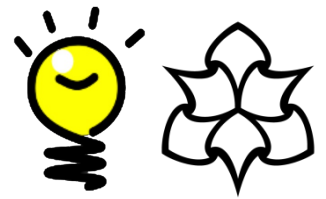
# Possible Generators for Exploration



Different (combinations of)...

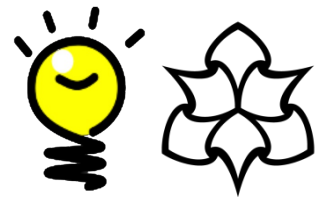
- neighbourhood functions
- kinds&levels for the satisfaction predicate
- distinct kinds of property
- numbers of each kind of agent
- movement algorithms
- number of empty spaces
- initial locations

# Specific Implementation



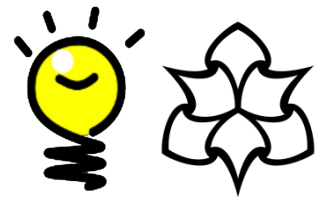
- If outcomes using a particular generator rarely make much difference then, replace it with a specific, fast algorithm
  - e.g. initial locations decided randomly
- If any are known or determined by target problem, replace generator with appropriate algorithm
  - e.g. if social structure of links is known, use that

# What have we achieved?



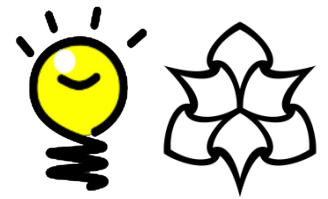
- Separated out the declarative specification and the imperative code...
- ...which can be the more essential assumptions and the more specific ones
- It allows a more incremental implementation approach with more checking included
- The declarative specification can be published separately so others can use it to:
  - explore the space of possibilities, knowing it is the same space
  - try their own imperative variants (and if they need to change the fundamentals, this triggers a different kind of debate)

# Rather than 1001 varieties...



We might be able to...

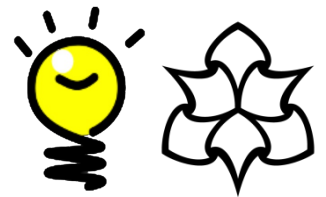
- find what general properties are essential to get target results and thus know when it might be applicable to observed cases
- avoid specific implementations that have bugs or are very brittle (require fine tuning for results)
- know how to standardise either declarative properties or implementations of parts (like movement or neighbourhood)



# Conclusions

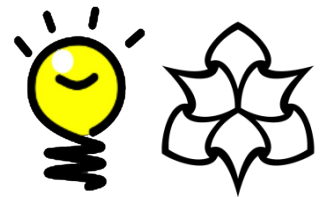


# Hope of Better Reliability



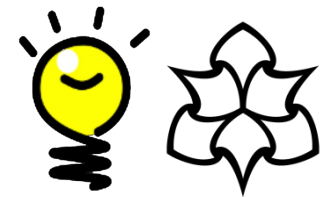
- Better, and more flexible, internal checking
- Separable declarative descriptive & checking layer that can be verified by others
- Earlier proof-of-concept enables to check the direction with others (e.g. stakeholders)
- Separation of code representing core assumptions with implementation specifics
- Clearer theory development with necessary conditions for results established

# Facilitating working as a Community



- Standard definitions of entities and relationships can be developed
- Declarative specifications may help check compatibility of models when joining them (and so help avoid “integronsters”)
- It may allow libraries of model components to be more reliable and easier to find (by some automation of which will work) and thus help with modelling for crises
- Interaction about abstractions and specifications can happen separately to those of implementations – e.g. aiding tool add-ons

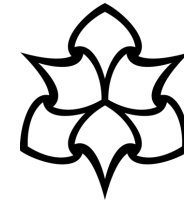
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