



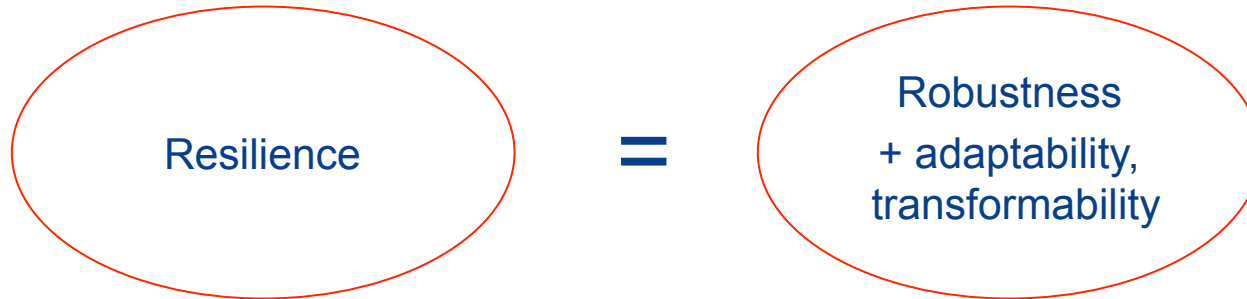
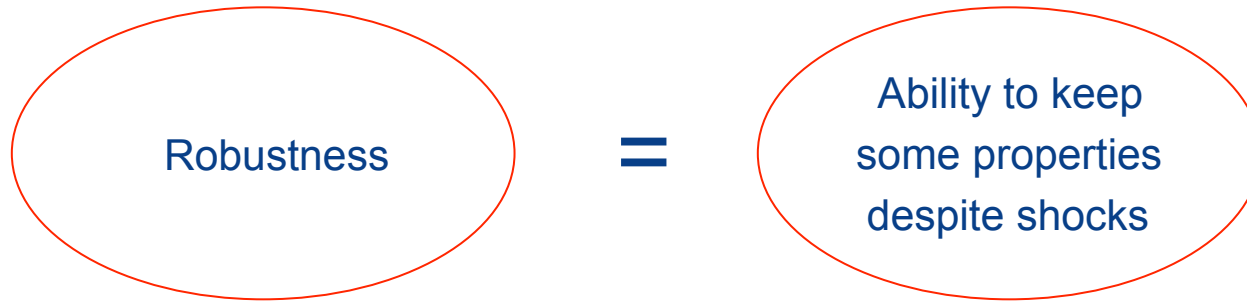
# Resilience, robustness and viability

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Irstea, France

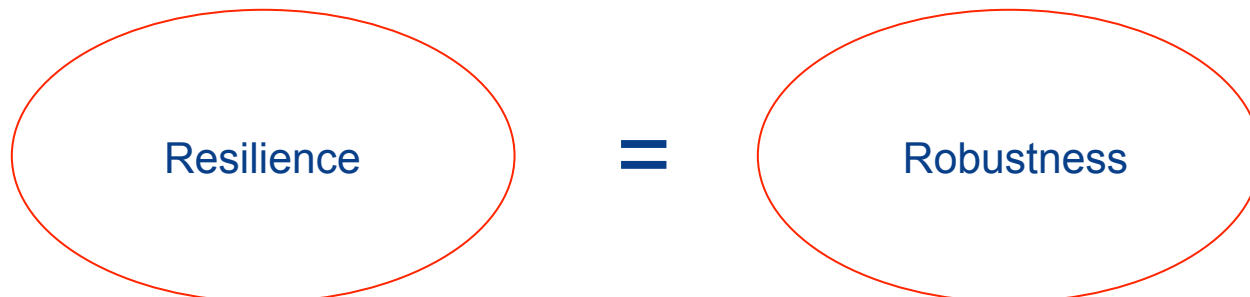


# Are resilience and robustness the same?

For Anderies, Folke, Walker, Oström 2013:



Since adaptability and transformability are particular dynamics then:





This is true but it's a pity!



- Indeed, resilience is most of the time considered as the same as robustness

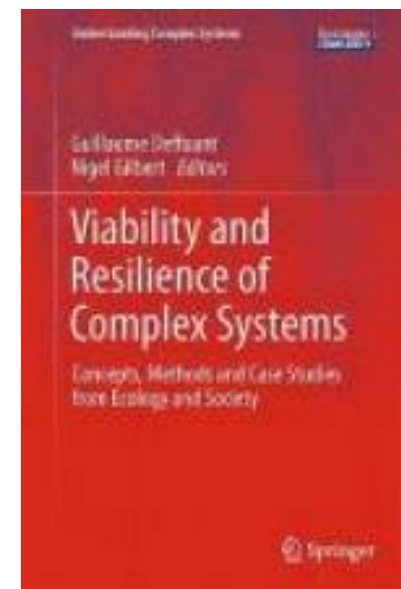
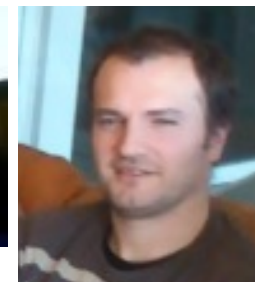
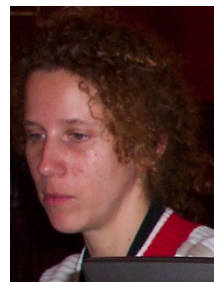
But:

- If the concepts are the same why using resilience and not robustness?
- This view misses an important part of the intuitive concept of resilience : **the ability to recover properties after having lost them**

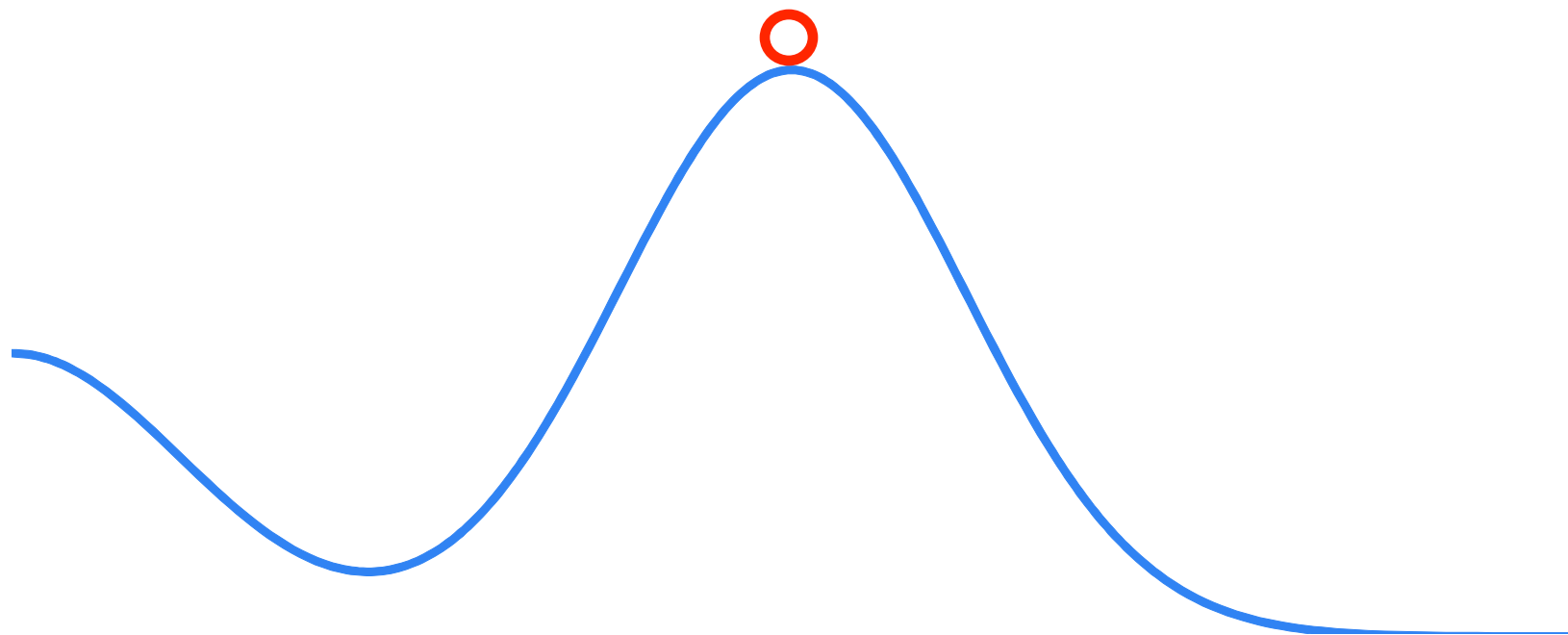
# Formalising resilience with viability theory

Using viability theory (Aubin 1991, 2011)

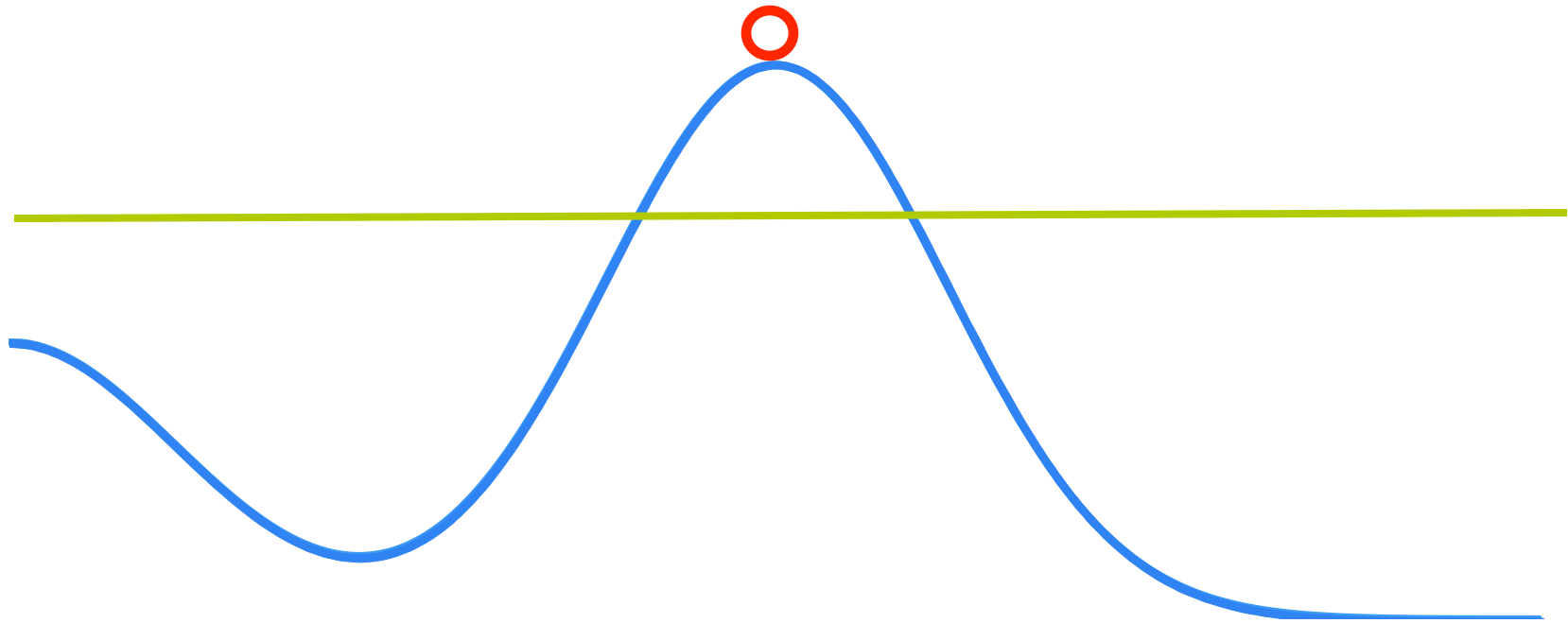
- Béné, Doyen, Garbay 2001
- Martin 2004
- Deffuant & Gilbert 2011
- Rougé, Mathias, Deffuant 2013, 2014



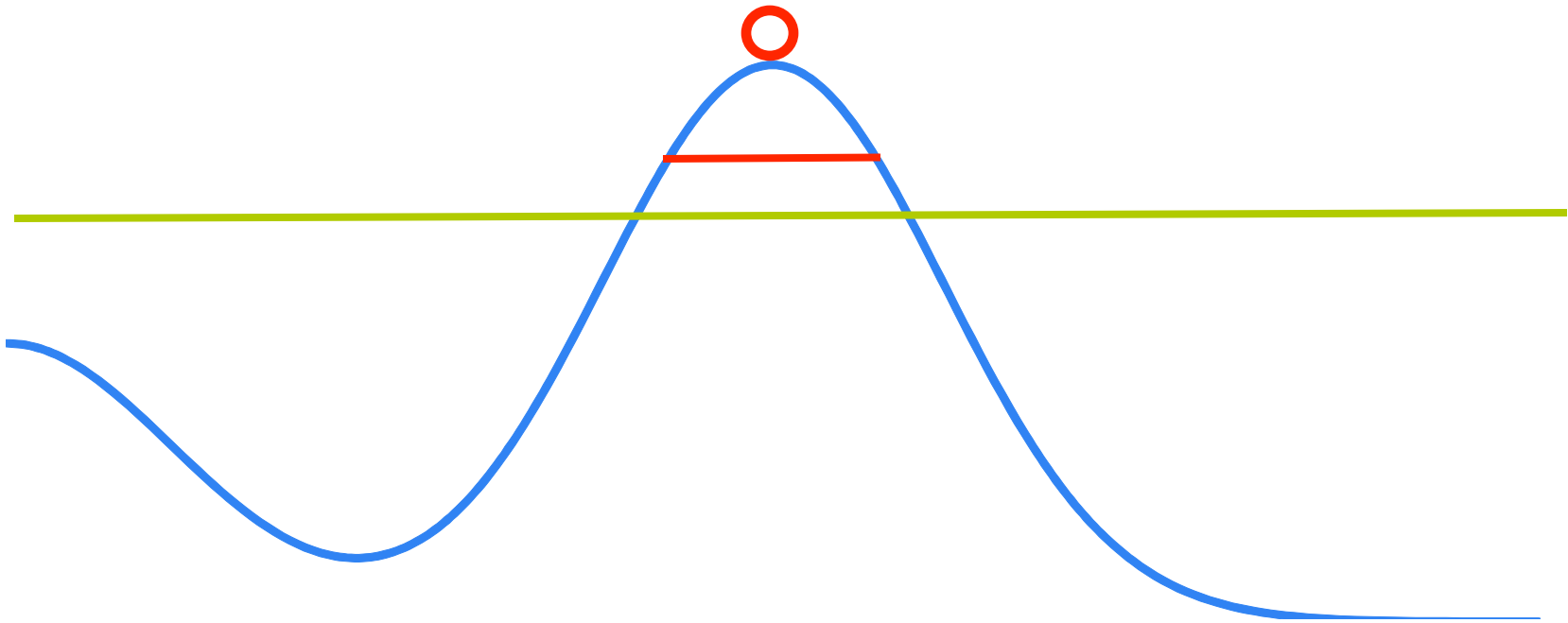
## Toy example 2: mobile ball on hills



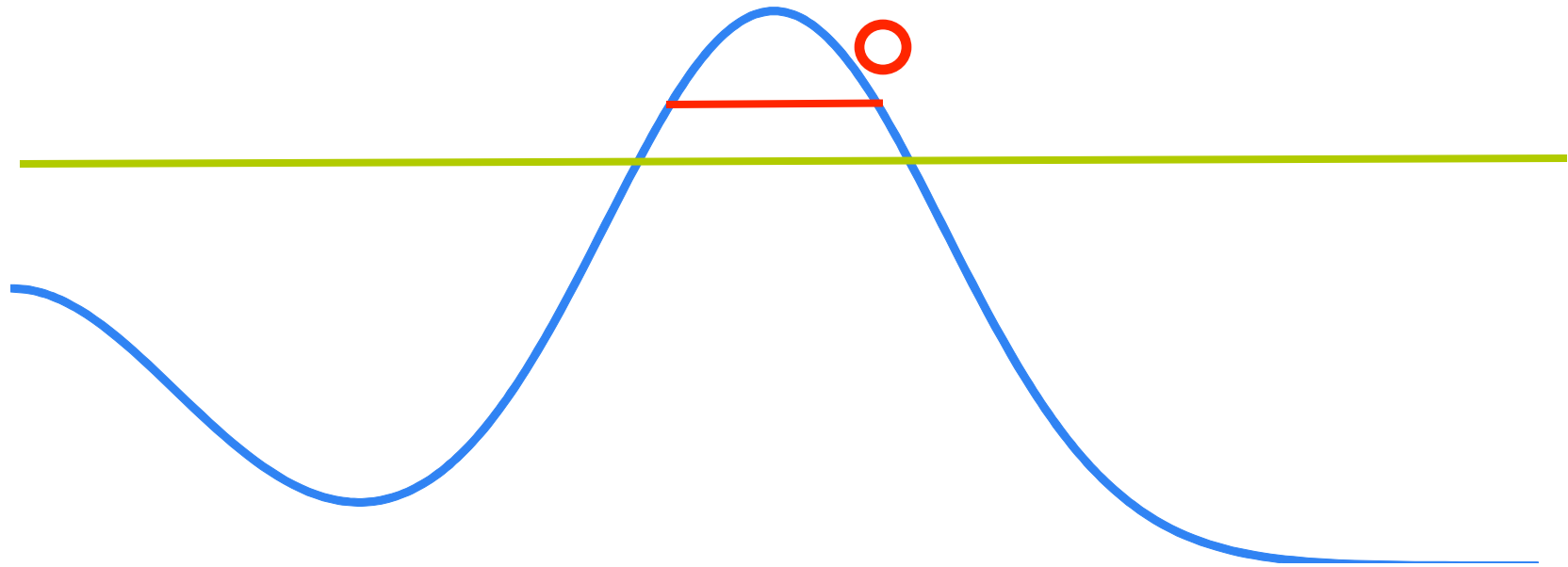
Property: the ball is above the green line



# Limit perturbations for robustness (ball with engine inside)

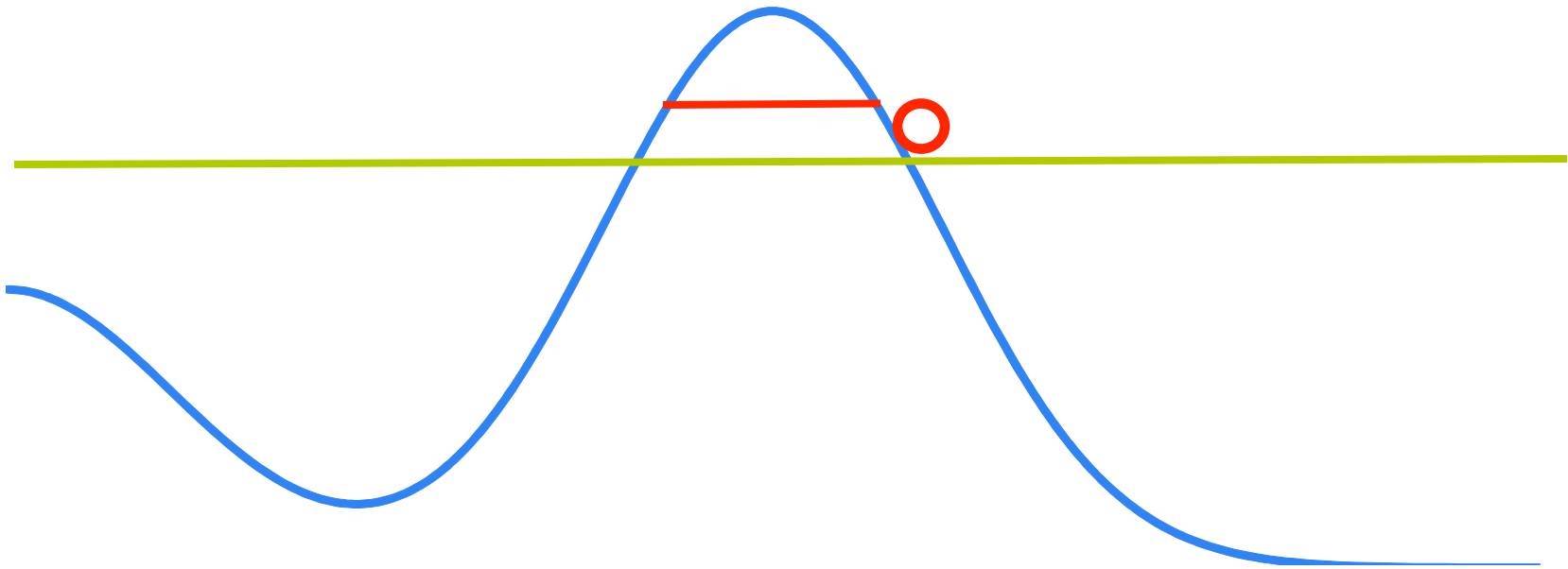


# Limit perturbations for robustness

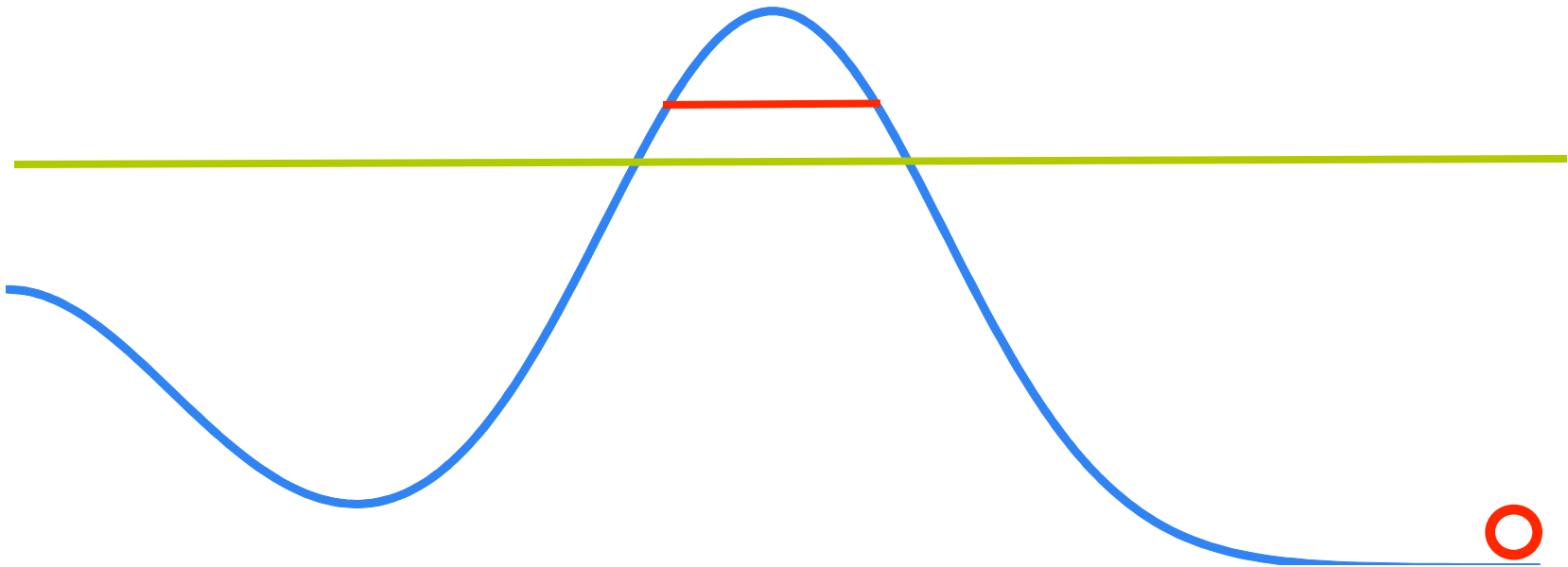




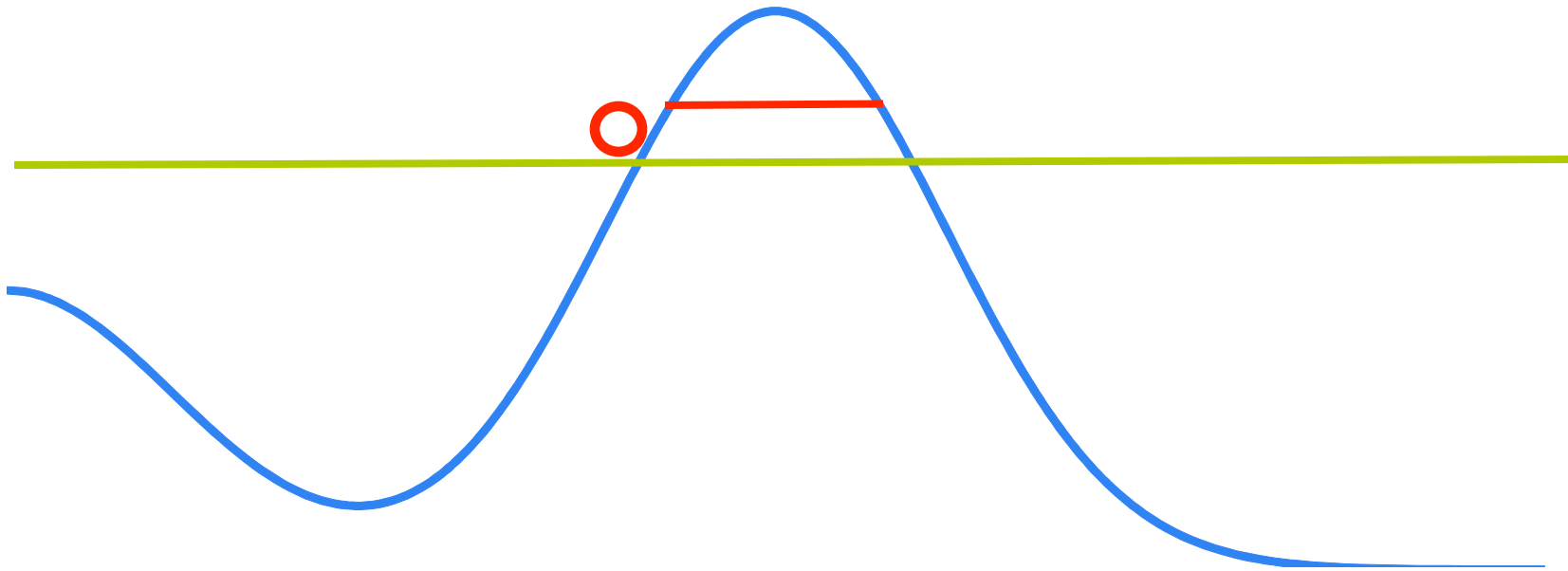
# Limit perturbations for robustness



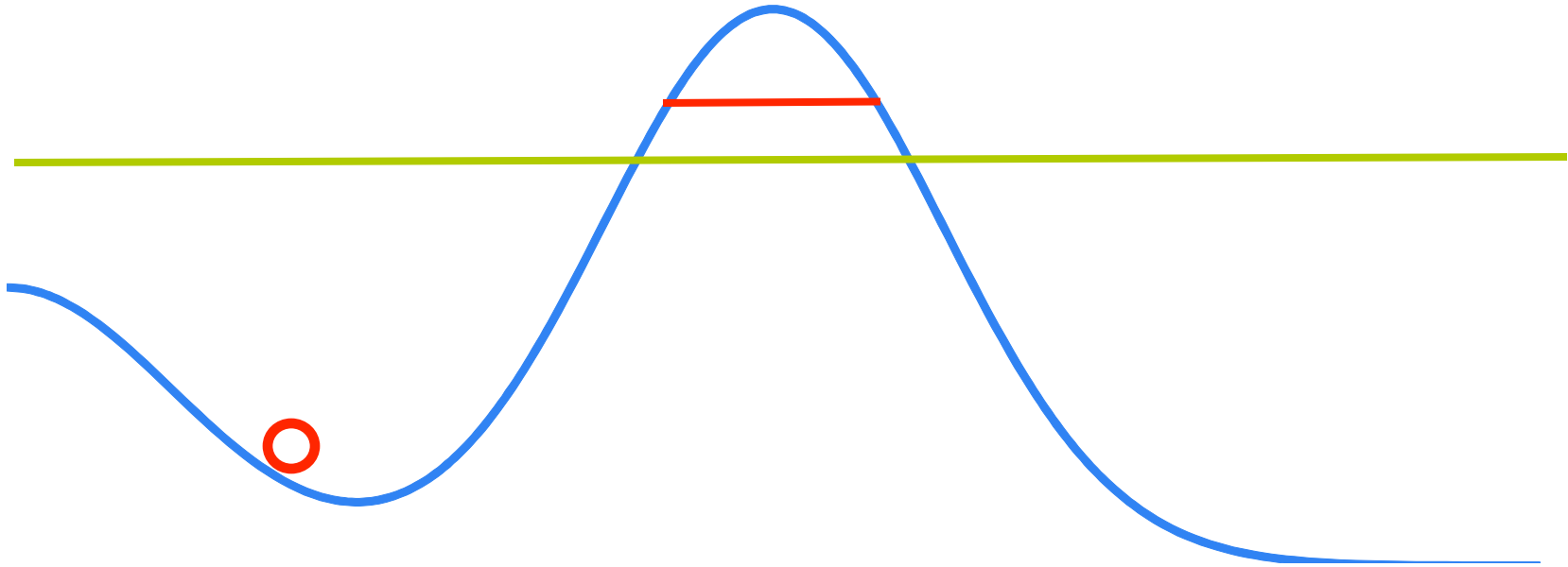
# Cannot recover the property



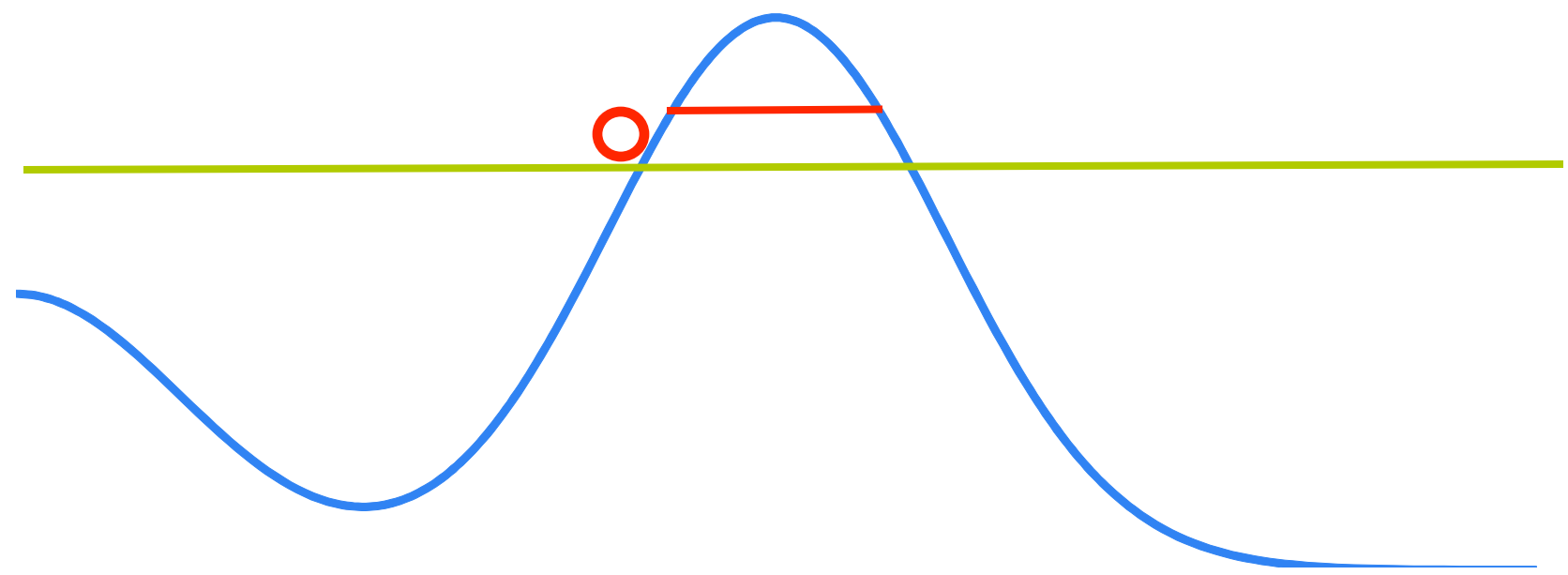
# Trajectory when braking all the way



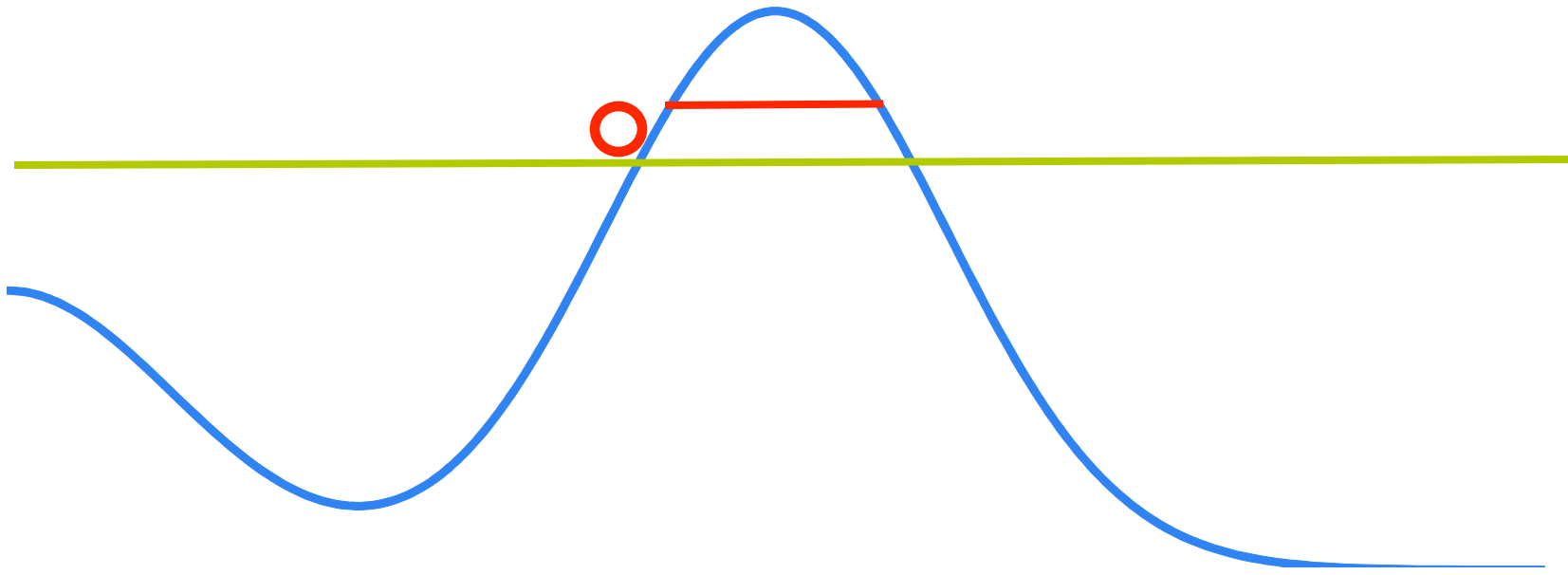
Can recover the property but cannot keep it



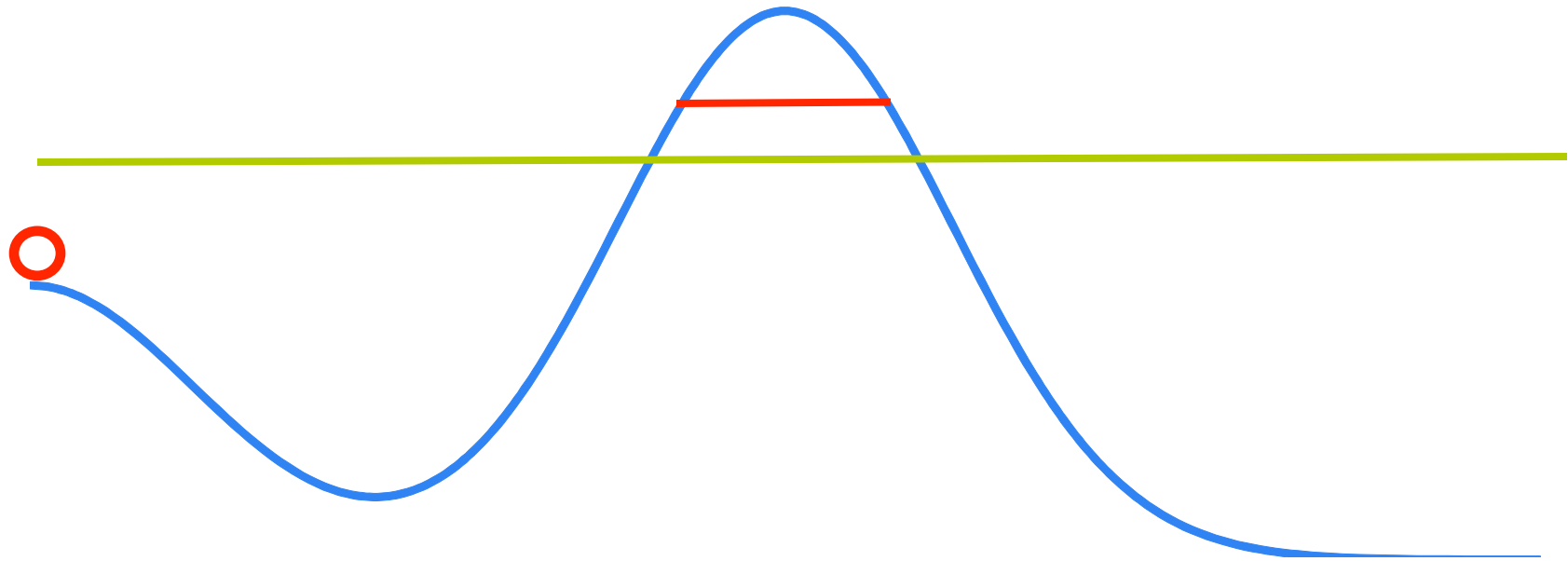
# The ball falls again



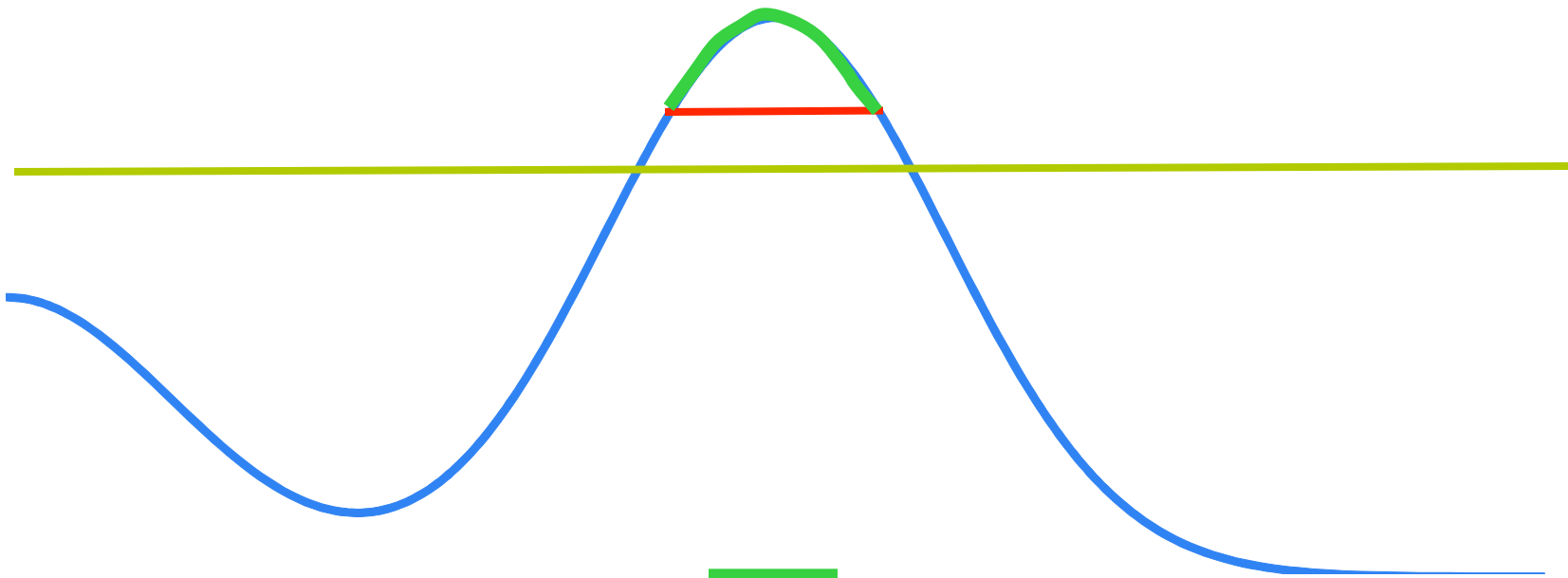
# Trajectory without slowing down



The mobile can then recover the property and keep it



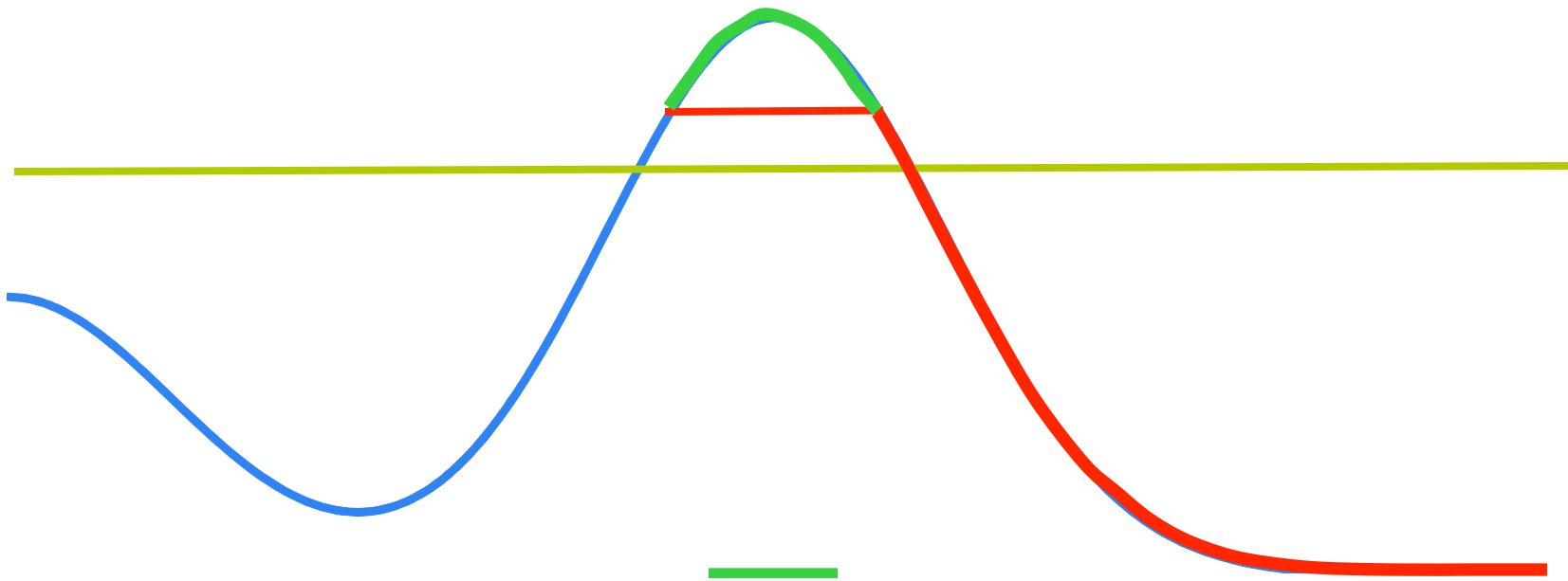
# Robustness and viability



The property is  
robust to the  
perturbations



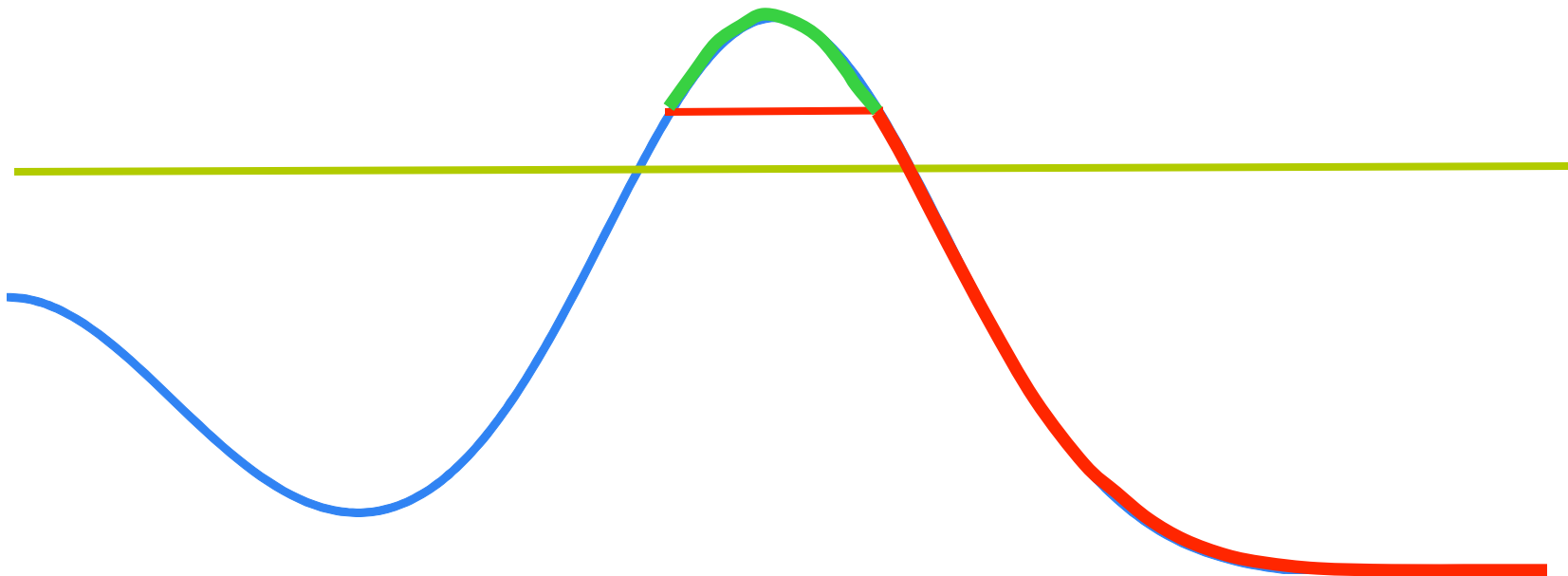
# Property is not resilient



The property can be kept (robust)

The property cannot be recovered : it is non resilient

# Property is resilient



The property can be recovered and kept: it is resilient

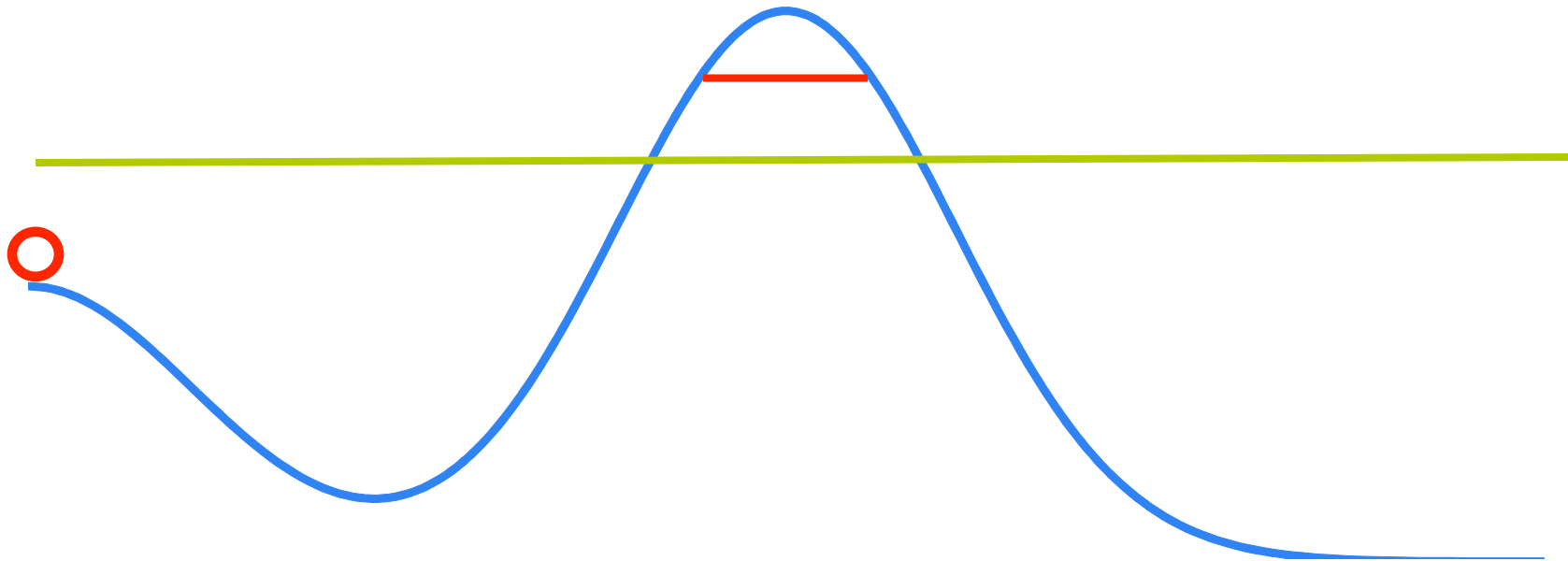


The property is kept (robust)



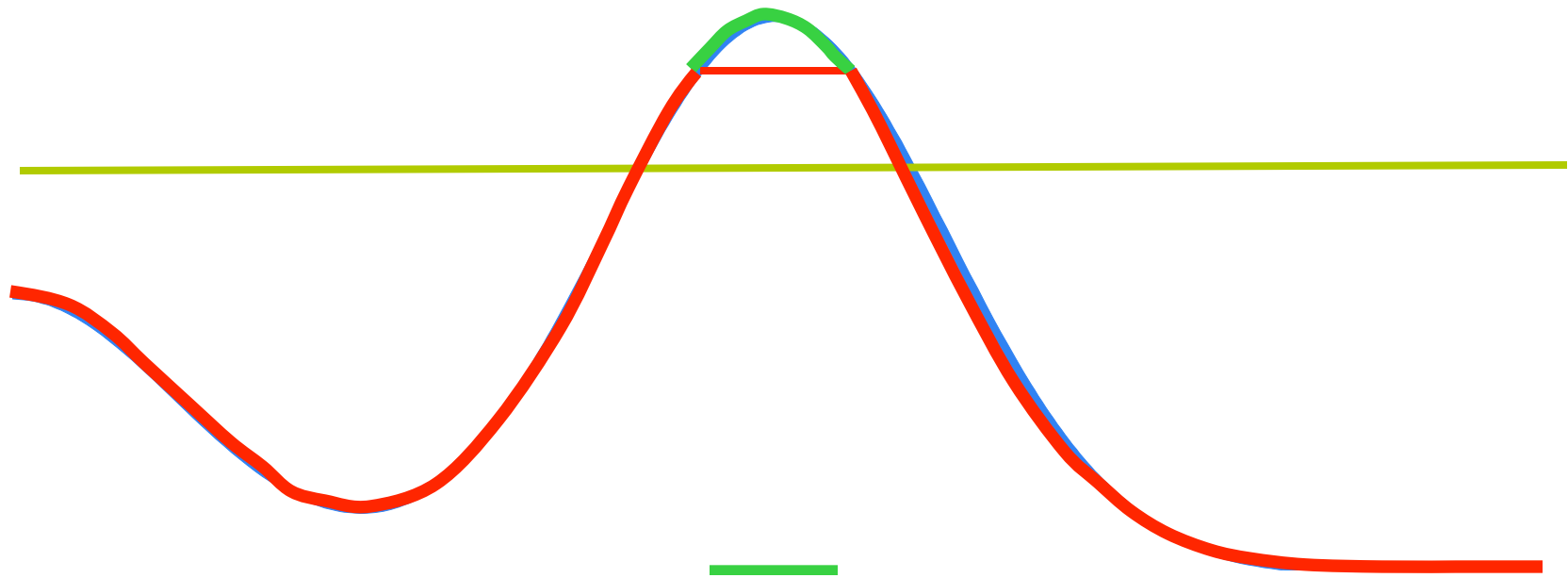
The property cannot be recovered : it is non resilient

# The engine is a bit less powerful



The system gets the property back but cannot keep it.  
It is not resilient.

# Property is not resilient

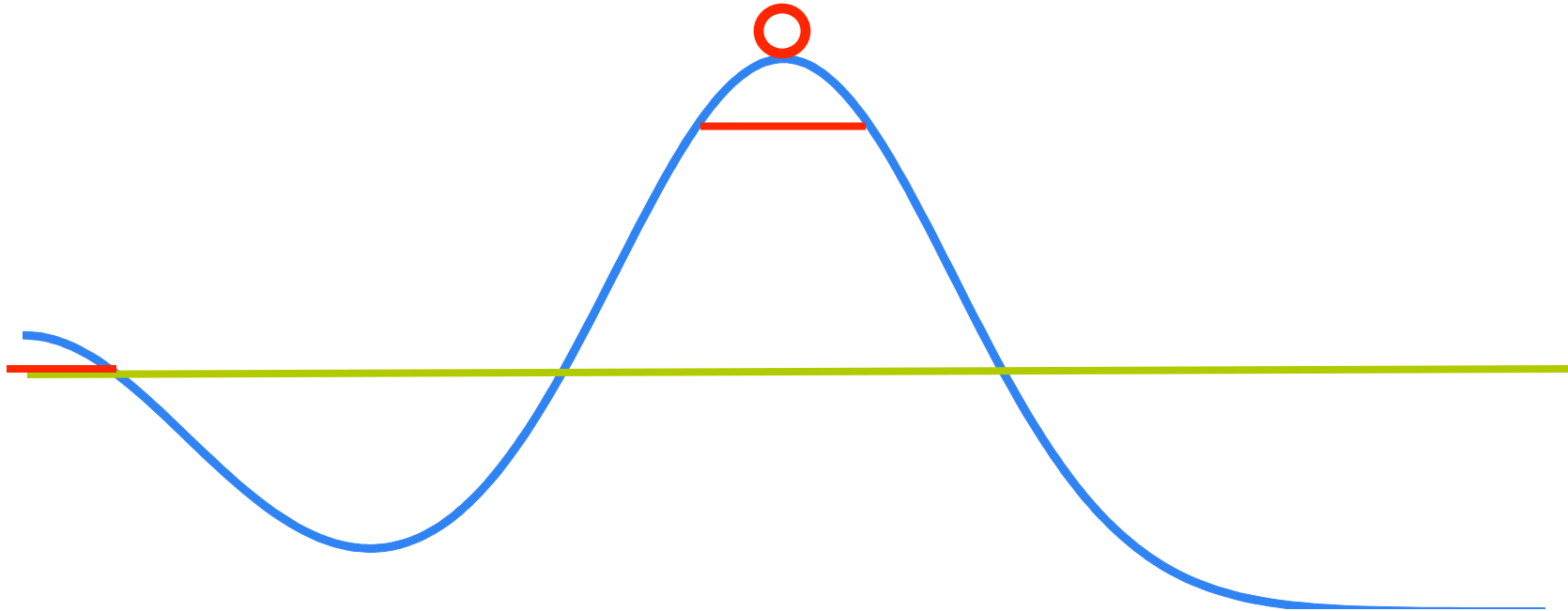


The property can come back to a robust state: it is resilient

The property is robust to the perturbations

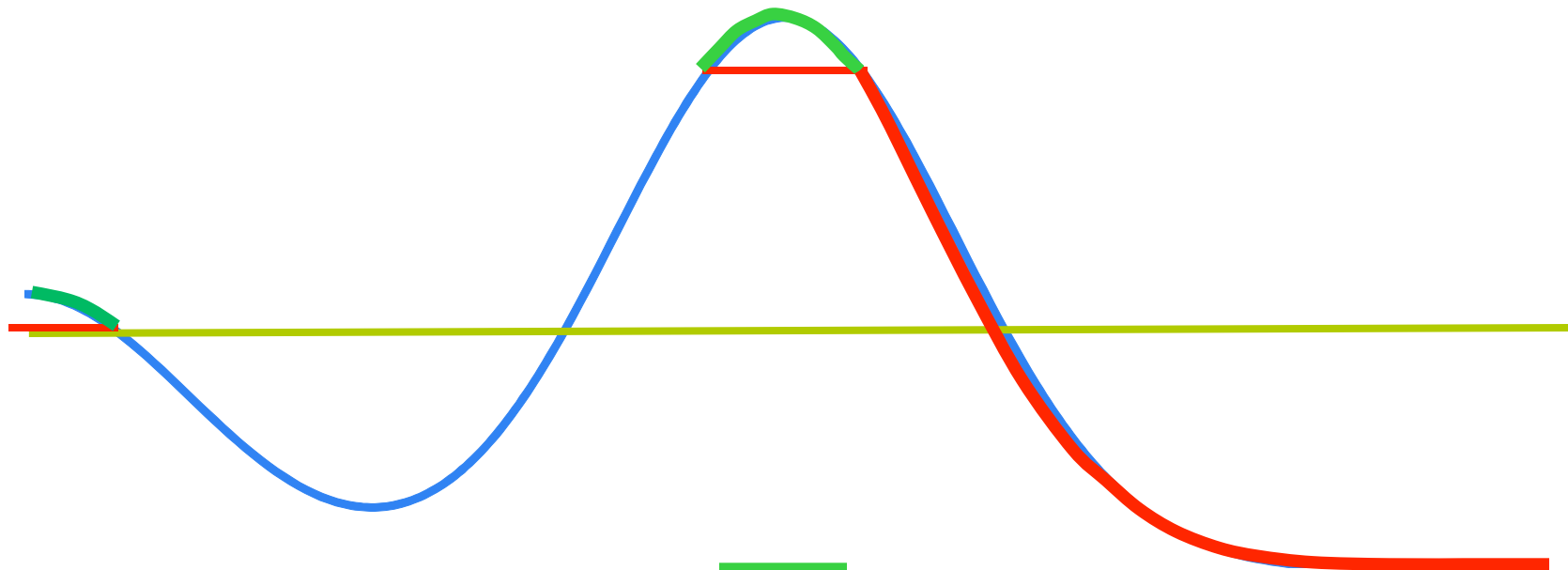
The property cannot be recovered : it is non resilient

# Changing the property




The system gets the property back but in an other state and it cannot get back to its initial point

# A part of the space becomes resilient again



  
The property can be recovered and kept: it is resilient

  
The property is kept (robust)

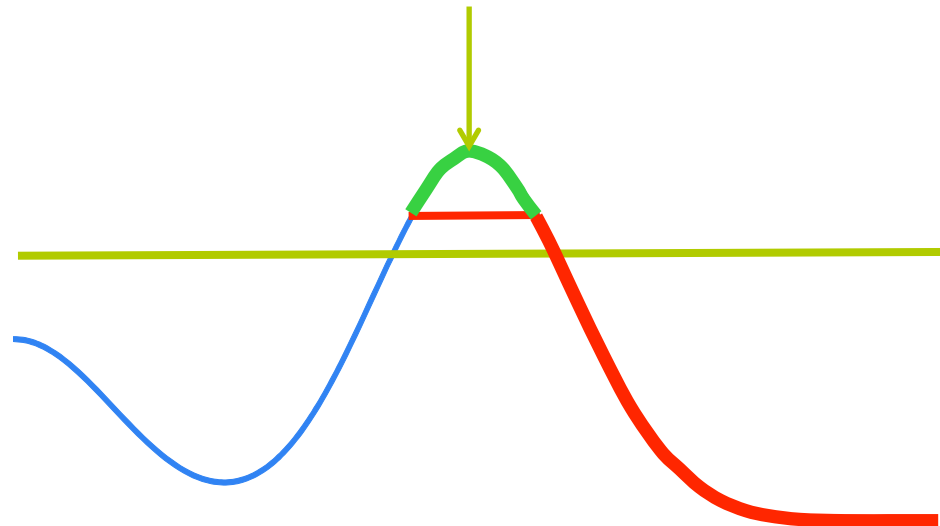
  
The property cannot be recovered : it is non resilient

## Viability kernel (of a property)

- The states of the system from which it can keep the property forever (without perturbations)

=

- The post-perturbation states from which the property can be kept forever

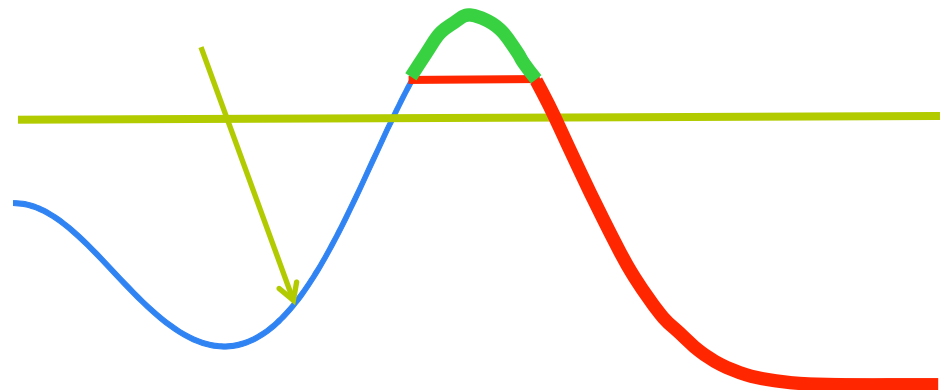


## Resilience basin (of a property)

- The states of the system from which the viability kernel can be reached (without perturbations)

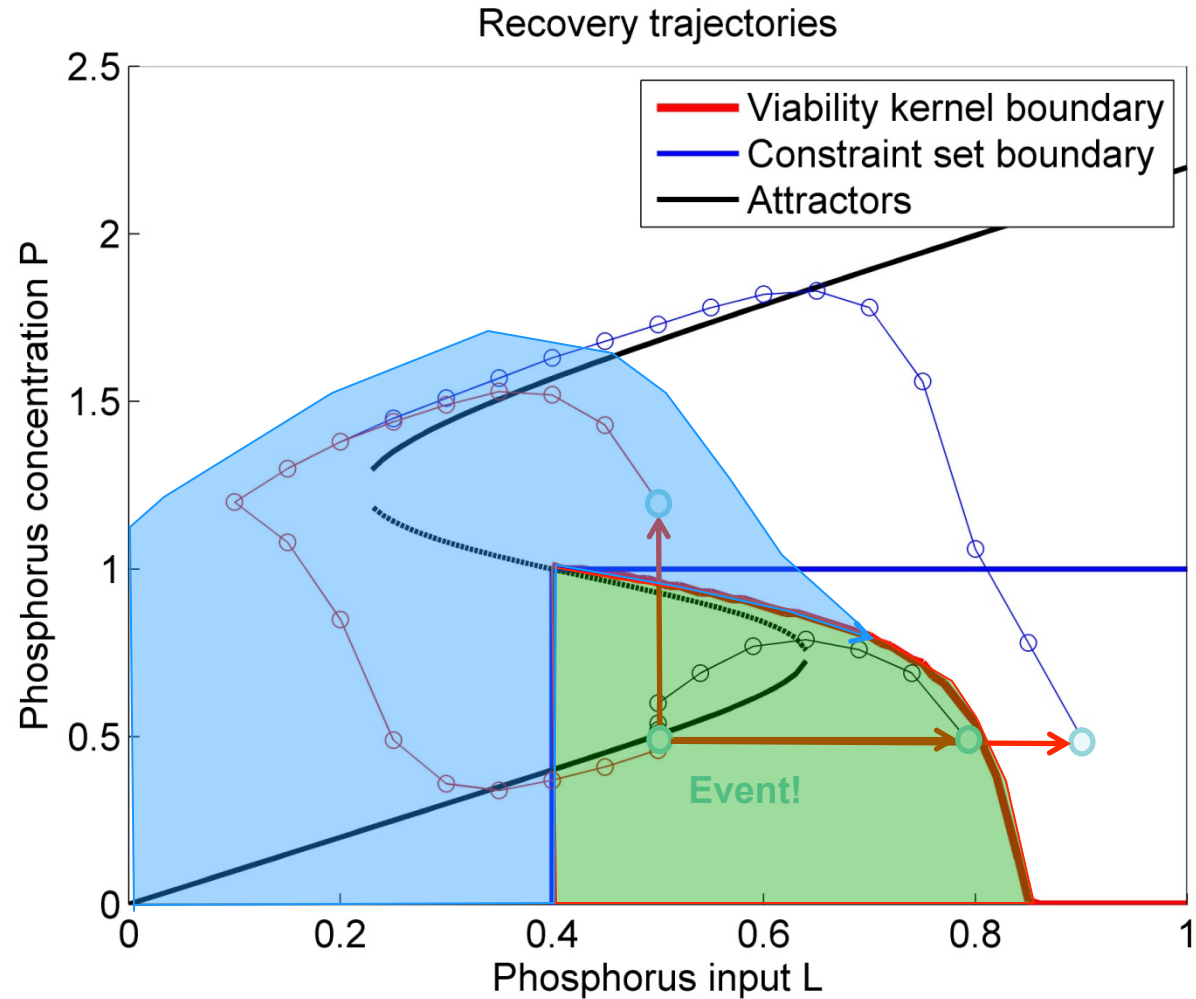
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- The post-perturbation states from which the property recovered and kept forever (without perturbations)

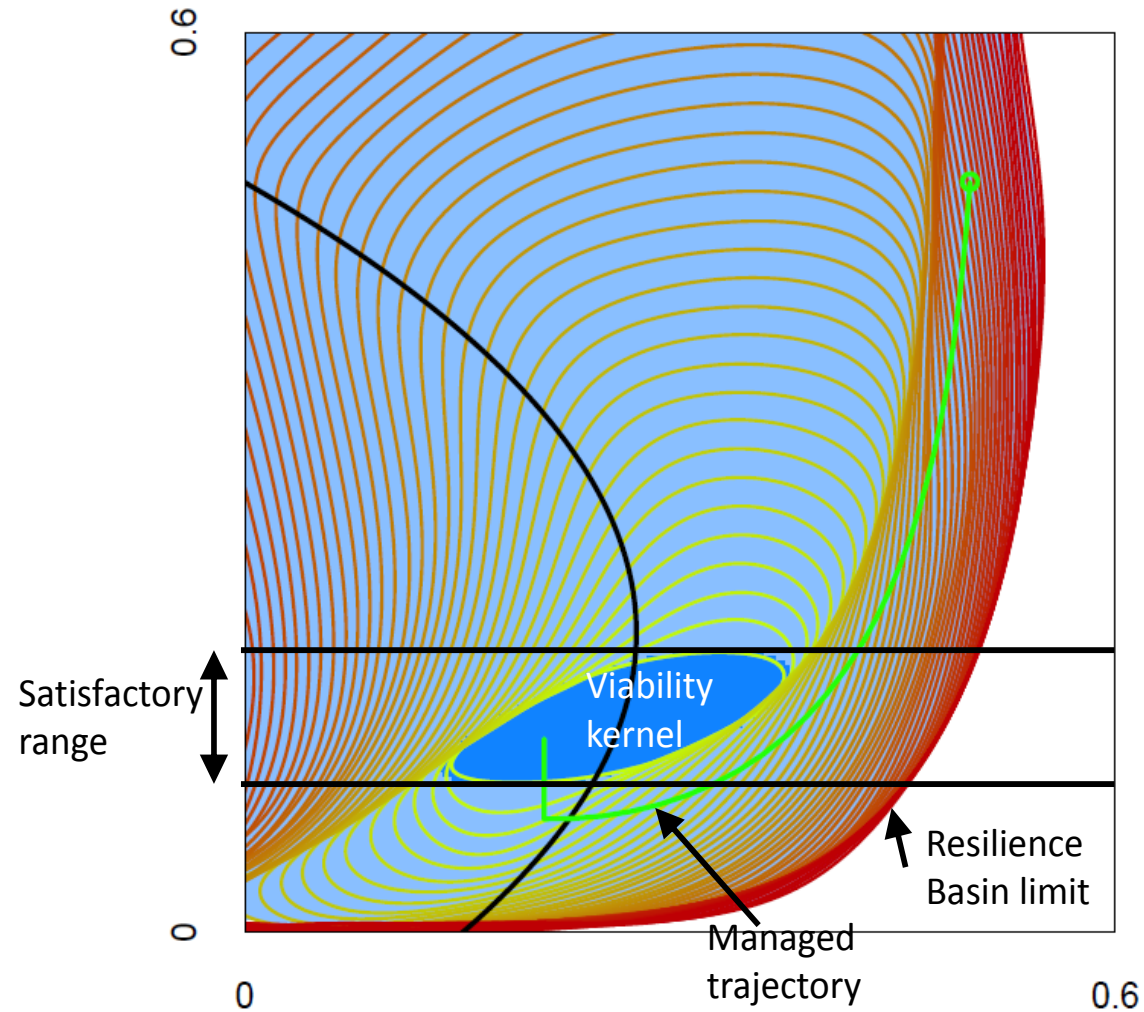




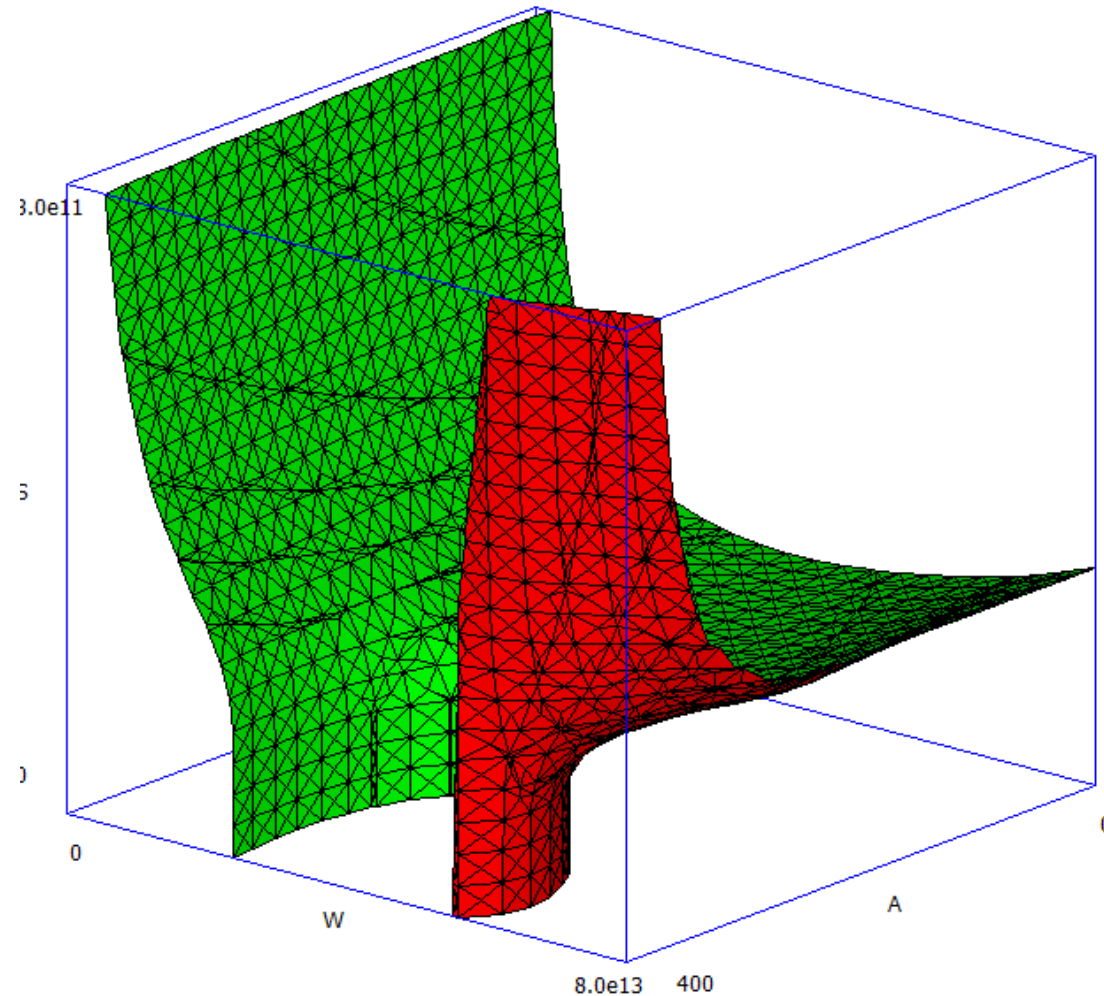
# Example based on lake dynamics model



# Example based on savannah dynamics model



# Example CO<sub>2</sub> in atmosphere (Viability kernel for 3D simple model)



## Different problems to be addressed

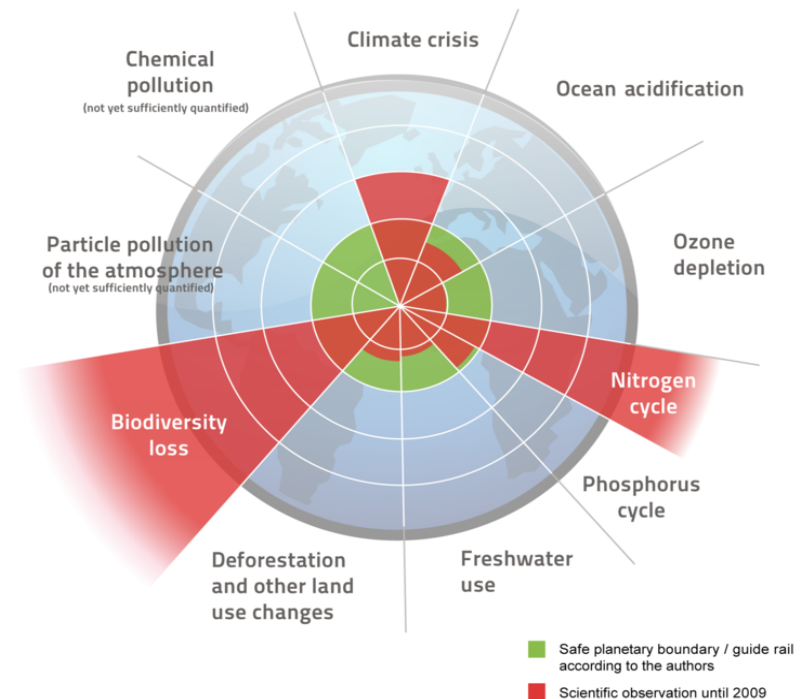
- Defining the property to be kept (political & scientific problem)
- Defining the envisaged actions on the system (political & scientific problem)
- Defining the state space of the model and the dynamics when applying the different actions over time (scientific problem: modelling)
- Determining the sequences of actions to apply in order to keep or recover the property (scientific problem: control theory)



Same distinctions in control theory approach, but

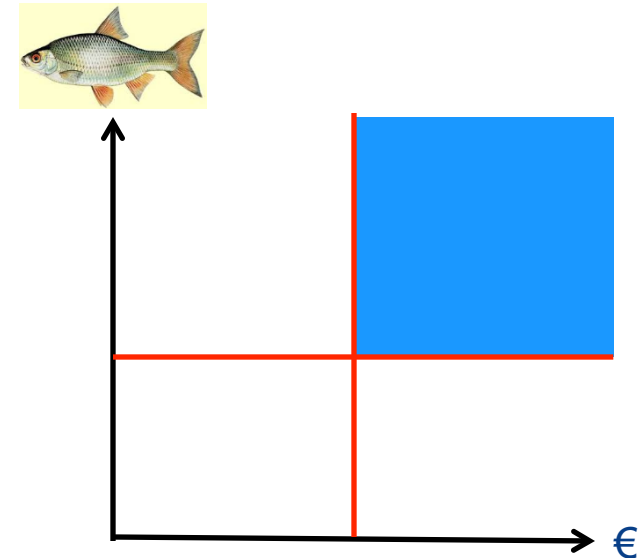
# The property is defined by constraints in state space

- Maastrich criteria: (3% GDP deficit, 60% GDP debt). Political choice; Submitted to referendum in several member states in 1992.
- Planetary boundaries (Rockstöm et al): based on evaluation by scientists of risk of shift to dangerous regime. Are planetary boundaries the property to be kept or an estimation of the viability kernel ?



## Multi-criteria without aggregation

- In usual control theory when the goal is multi-criteria, then need to aggregate using weights
- The property to be kept in viability approach can be defined as the intersection of different constraints e.g. economic and environmental



## No discount rate over time

- In usual control theory the goal is to the sum of future gains:

$$G = \sum_{t=0}^{\infty} g(t) e^{-\delta t}$$

- Depending on this discount rate, it can be rational to over-exploit and destroy a resource
- There is no necessity of such a discount rate in viability theory: keeping the property can be as important in the future as it is now

# Current developments

- Including uncertainties into the framework
- Connecting the framework with socio-ecological and coupled infrastructure systems
- Including the possibility of different control regimes (no control, standard and emergency for instance). See Heitzig et al. 2016

